

# MATHEMATICS SSC-II ( $\mathbf{3}^{\text {rd }}$ Set) 

(Science Group) (Curriculum 2006)
SECTION - A (Marks 15)
Time allowed: 20 Minutes
Section - A is compulsory. All parts of this section are to be answered on this page and handed over to the Centre Superintendent. Deleting/overwriting is not allowed. Do not use lead pencil.

## Q. 1 Fill the relevant bubble for each part. All parts carry one mark.

(1) Cancellation of $x$ on both sides of $6 x^{2}=21 x$ means:
A. The loss of one root
B. No loss of any root
C. The gain of one root
D. Undefined solution

(2) If $b^{2}-4 a c>0$ is a perfect square then roots of $a x^{2}+b x+c=0$ are?
A. Irrational, Equal
B. Rational, Equal
C. Rational, Unequal
D. Irrational, Unequal
(3) On simplifying $\left(7+5 \omega+5 \omega^{2}\right)^{2}$ we get:
A. $\quad 4$
B.
12
D. 144
(4) If $y^{2}$ varies inversely as $x^{3}$ then:
A. $y^{2}=k x^{3}$
$\bigcirc$
B. $y^{2}=\frac{k}{x^{3}}$
C. $\frac{y^{2}}{x^{3}}=1$
D. $y^{2} x^{3}=1$
(5) Partial fractions of $\frac{x^{2}+1}{(x+1)(x-1)}$ are of the form:
A. $\quad 1-\frac{A}{(x+1)}+\frac{B}{(x-1)}$
B. $1+\frac{A}{(x+1)}+\frac{B}{(x-1)}$
C. $1+\frac{A}{(x+1)}+\frac{B x}{(x-1)}$
D. $\frac{A}{(x+1)}+\frac{B}{(x-1)}$
(6) If $A \cap B=\emptyset$, then set A and B are:
A. Subsets of each other
B. Overlapping sets
C. Disjoint sets
D. Equal sets


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(7) If $f: A \rightarrow B$ and range of $f \neq B$ then $f$ is a/an:
A. Into functionB. Onto function
C. Bijective function
D. Injective function
(8) If $Y=X+5$ then $\bar{Y}=$ ?
A. $\bar{X}$B. 5
C. $\bar{X}+5$
D. $5 \bar{X}$
(9) $\quad \sum(X-\bar{X})=$ ?
A. 2
C. -1
$\bigcirc$
B. 1
D. 0
(10) In which of the following quadrants $\theta$ lies when $\sin \theta<0, \sec \theta<0$ ?
A. I
B. II
C. III
D. IV
$\bigcirc$
(11) $\sec \theta \cot \theta=$ ?
A. $\operatorname{cosec} \theta$B. $\tan \theta$
C. $\sin \theta$
D. $\cos \theta$
(12) What is the value of $m$, if $r=15$ and $\theta=\frac{\pi}{3}$ ?
A. $5 \pi$B.
D. $\frac{45}{\pi}$

(13) What is the length of chord intercepted at 4 cm away from the centre of the circle?
A. 4 cm
B. 6 cm
C. $\quad 7 \mathrm{~cm}$
D. 9 cm

(14) If $\overline{D C} \| \overline{A B}$ and $\angle A O C=100^{\circ}$ (in the figure), then $\angle A C D=$ ?
A. $\quad 30^{\circ}$

B. $40^{\circ}$
C. $50^{\circ}$
D. $60^{\circ}$
(15) In the adjoining figure, length of the escribed radii $a$ is:
A. $a$
O
B. $2 a$
C. $3 a$
$\bigcirc$
D. $\frac{1}{2} a$


Note: Attempt any nine parts from Section 'B' and any three questions from Section 'C' on the separately provided answer book. Write your answers neatly and legibly. Log book will be provided on demand.

## SECTION - B (Marks 36)

Q. 2 Attempt any NINE parts from the following. All parts carry equal marks. $(9 \times 4=36)$
i. Apply quadratic formula to solve the equation $\frac{2 x+1}{x+2}-\frac{2 x+4}{2 x+8}=\mathbf{0}$
ii. Find the value of $x: \quad 3.3^{2 x+1}-10.3^{x}+1=0$
iii. If $\theta$ and $\varphi$ are the roots of $y^{2}-7 y+9=0$. Form an equation whose roots are $2 \theta$ and $2 \varphi$.
iv. The length of a rectangle is 5 cm more than its breadth. If the area of the rectangle is $50 \mathrm{~cm}^{2}$, find its length and breadth.
v. Find the fourth proportional to: $\left(x^{3}-y^{3}\right),\left(x^{2}-y^{2}\right),\left(y^{2}+2 x y+y^{2}\right)$
vi. The current I in a wire varies directly as electromotive force E, and inversely as resistance R. If $I=32$ amperes, when $E=1280$ volts and $R=80$ ohms, what will be the value of I when $\mathrm{E}=1500$ volts and $\mathrm{R}=180$ ohms?
vii. Resolve $\frac{4 x+2}{2(x-1)\left(x^{2}+1\right)}$ into partial fractions.
viii. If $\mathrm{U}=\{1,2,3, \ldots, 20\}, \mathrm{A}=\{1,2,3, \ldots, 10\}$ and $\mathrm{B}=\{2,4,6,8,10,12,14,16\}$, then find $(A \cup B)-(A \cap B)^{c}$
ix. The marks of four students in Mathematics are as follows. Determine Variance and Standard Deviation.

| Students | 1 | 2 | 3 | 4 |
| ---: | ---: | ---: | ---: | ---: |
| Marks | 90 | 80 | 70 | 90 |

x. If $\tan \theta=\frac{\sqrt{7}}{2}$, then find the values of other trigonometric ratios.
xi. Prove that, the perpendicular from the center of a circle on a chord bisects it.
xii. $\quad \overrightarrow{P A}$ and $\overrightarrow{P B}$ are tangents to the circle from an external point $P$.
$\overline{C D}$ is another tangent touching the circle at E such that
$m \overline{C E}=m \overline{D E}=2 \mathrm{~cm}$.
If $m \overline{P A}=8 \mathrm{~cm}, m \overline{O A}=3 \mathrm{~cm}$ then, find $m \overline{P C}+m \overline{P D}$.

xiii. In the adjoining figure, ABCD is a cyclic quadrilateral inscribed in a circle having centre at O .
If $a=30^{\circ}, d=45^{\circ}$, then find the values of $b, c, e$ and $f$.
xiv. Prove that, equal chords of a circle subtend equal angles at the centre.

## SECTION-C (Marks-24)

NOTE: Attempt any three questions. All questions carry equal marks. $\quad(\mathbf{3} \times \mathbf{8}=\mathbf{2 4})$
Q. 3 Solve the equation: $x^{4}-4 x^{3}-3 x^{2}+4 x+1=0$
Q. 4 Verify De-Morgan's Laws for the following sets:

$$
U=\{x \mid x \in N \wedge 5 \leq x \leq 20\}, A=\{x \mid x \in E \wedge 5 \leq x \leq 20\}, B=\{x \mid x \in P \wedge 5 \leq x \leq 20\}
$$

Q. 5 For the following frequency distribution

| Classes | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 3 | 4 | 5 | 6 | 7 |

a. Calculate Geometric Mean of the data.
b. Calculate Harmonic Mean of the data.
Q. 6 Circumscribe a regular hexagon about a circle of radius 5 cm .
Q. 7 In any triangle, the sum of the squares on any two sides is equal to twice the square on half the third side together with twice the square on the median which bisects the third side (Apollonius' Theorem).

# MATHEMATICS SSC-II ( ${ }^{\text {rd }}$ Set) Student Learning Outcomes Alignment Chart 

Science Group (Curriculum 2006)

| Sec-A | Q 1 | Contents and Scope | Student Learning Outcomes |
| :---: | :---: | :---: | :---: |
|  | i | 8.2 Solution of Quadratic Equations | Solve a quadratic equation in one variable by factorization |
|  | 11 | 9.1 Nature of the Roots of a Quadratic Equation | iii) Discuss the nature of roots of a quadratic equation through discriminant |
|  | iii | 9.2 Cube Roots of Unity and their Properties | iv) Use properties of cube roots of unity to solve appropriate problems. |
|  | iv | 10.1 Ratio, Proportions and Variations | i) Define ratio, proportions and variations (direct and inverse). |
|  | v | 11.2 Resolution of Fraction into Partial Fractions. | Resolve an algebraic fraction into partial fractions when its denominator consists of non-repeated linear factors. |
|  | vi | 12.1.3 Venn Diagram | i) Use Venn diagram to represent <br> - union and intersection of sets, <br> - complement of a set. |
|  | vii | 12.3 Function | i) Demonstrate the following: <br> - into function, <br> - one-one function, <br> - into and one-one function <br> (injective function), <br> - onto function (surjective function), <br> - one-one and onto function (bijective function). |
|  | viii | 13.3 Measures of Central Tendency | ii) Recognize properties of arithmetic mean. |
|  | ix | 13.3 Measures of Central Tendency | i) Calculate (for ungrouped and grouped data): <br> - Arithmetic mean by definition and using deviations from assumed mean. |
|  | X | 16.3 Trigonometric Ratios | v) Recognize signs of trigonometric ratios in different quadrants. |
|  | xi | 16.4 Trigonometric Identities | Prove the trigonometric identities and apply them to show different trigonometric relations. |
|  | xii | 16.2 Sector of a Circle | i) Establish the rule $l=r \theta$ where $r$ is the radius of the circle, $l$ the length of circular arc and $\theta$ the central angle measured in radians. |
|  | xiii | 25.1 Chords of a Circle | ii) A straight line, drawn from the centre of a circle to bisect a chord (which is not a diameter) is perpendicular to the chord. |
|  | xiv | 28.1 Angle in a Segment of a Circle | i) The angle <br> - in a semi-circle is a right angle, <br> - in a segment greater than a semicircle is less than a right angle, |


|  |  |  | - in a segment less than a semi- <br> circle is greater than a right angle. |
| :---: | :---: | :--- | :--- |
|  | xv | 30.2 Circles attached to Polygons | iii) Escribe a circle to a given triangle. |$|$| Sec B | Q2 | 8.3 Quadratic Formula |
| :--- | :--- | :--- |
|  | ii | 8.4 Equations Reducible to <br> Quadratic Form |
| quadratic equations. |  |  |


| Sec C |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Q 3 | 8.4 Equations Reducible to <br> Quadratic Form   | iii) Solve reciprocal equations of the type. $a\left(x^{2}+\frac{1}{x^{2}}\right)+b\left(x+\frac{1}{x}\right)+c=0$ |
|  | Q 4 | 12.1.2 Properties of Union and Intersection | iv) Give formal proofs of the following fundamental properties of union and intersection of two or three sets. <br> - De Morgan's laws. |
|  | Q 5 | 13.3 Measures of Central Tendency | i) Calculate <br> (for ungrouped and grouped data) <br> - Median, Mode, Geometric Mean, Harmonic Mean. |
|  | Q6 | 30.2 Circles attached to polygons | viii) Circumscribe a regular hexagon about a given circle. |
|  | Q 6 | 11.2 Resolution of Fraction into Partial Fractions | Resolve an algebraic fraction into partial fractions when its denominator consists of <br> - Repeated quadratic factors. |
|  | Q 7 | 24.1 Projection of a Side of a Triangle | iii) In any triangle, the sum of the squares on any two sides is equal to twice the square on half the third side together with twice the square on the median which bisects the third side (Apollonius' Theorem). |

## MATHEMATICS SSC-II (3 ${ }^{\text {rd }}$ Set)

Table of Specification

| Units |  |  |  |  |  |  |  |  |  | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { N N } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  |  |  | å |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Knowledge based |  | 1(2)(1) | 1(4)(1) |  | $\begin{gathered} \hline 1(6)(1) \\ 1(7)(1) \\ 4(8) \end{gathered}$ | 1(9)(1) |  | 7 (8) | 2 xi (4) |  | $2 \operatorname{xiv}$ (4) | 2 xiii (4) |  | 33 | 29.7\% |
| Comprehension based | $\begin{gathered} 1(1)(1) \\ 2 \mathrm{ii}(4) \\ 3(8) \end{gathered}$ | $\begin{aligned} & 1(3)(1) \\ & 2 \text { iii }(4) \end{aligned}$ | 2 v (4) | $\begin{gathered} 2 \text { vii (4) } \\ 1(5)(1) \end{gathered}$ | 2 viii (4) | $\begin{gathered} 1(8)(1) \\ 5(8) \end{gathered}$ | $\begin{gathered} 1(10)(1) \\ 1(11)(1) \\ 1(12)(1) \\ 2 \times(4) \end{gathered}$ |  |  |  |  |  | 6 (8) | 55 | 46.5\% |
| Application based | 2 i (4) | 2 iv (4) | 2 vi (4) |  |  | 2 ix (4) |  | V | 1(13)(1) | 2 xii (4) |  | 1(14)(1) | 1(15)(1) | 23 | 20.7\% |
| Total marks for each unit | 17 | 10 | 09 | 05 | 14 | 14 | 07 | 08 | 05 | 04 | 04 | 05 | 09 | 111 | 100\% |

## KEY:

1(1)(01)
Question No (Part No.) (Allocated Marks)
Note: (i) The policy of FBISE for knowledge based questions, understanding based questions and application based questions is approximately as follows:
a) $30 \%$ knowledge based.
b) $50 \%$ understanding based.
c) $20 \%$ application based.
(ii) The total marks specified for each unit/content in the table of specification is only related to this model question paper.
(iii) The level of difficulty of the paper is approximately as follows:
a) $40 \%$ easy
b) $40 \%$ moderate
c) $20 \%$ difficult

